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RESEARCH MEMORANDUM

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SOME CHARACTERISTICS OF ROLL CONTROLS HAVING POSSIBLE APPLICATION TO FIN-STABILIZED AMMUNITION

By Eugene D. Schult

Langley Aeronautical Laboratory
Langley Field, Va.

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NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

RESEARCH MEMORANDUM

SOME CHARACTERISTICS OF ROLL CONTROLS HAVING POSSIBLE APPLICATION TO FIN-STABILIZED AMMUNITION[1]

By Eugene D. Schult

SUMMARY

This paper discusses the rolling effectiveness of deflected fins, flaps, spoilers, and jet devices which may be employed on fin-stabilized ammunition. The possible applications and some of the significant factors affecting the performance of each device are described. The experimental information has been published previously and was obtained chiefly from free-flight tests conducted by the National Advisory Committee for Aeronautics on fin-stabilized vehicles at Mach numbers up to approximately 2.0. Comparisons are made in some cases with existing theory which is also relied upon to indicate trends where data are not available. This information is reviewed to emphasize points of possible interest to ammunition designers.

INTRODUCTION

The NACA is currently devoting a part of its research program to the problem of controlling slender, high-speed, missile configurations. A portion of this program which may be of interest to designers of fin-stabilized ammunition is the rolling effectiveness of various control devices which, if attached to the fins or body of a round, would incorporate roll in the flight path. The purpose of the present paper is to discuss deflected fins, flaps, spoilers, and air jets and their possible applications and to review briefly some of the significant factors that affect their performance. Theory is heavily relied upon to indicate trends where experimental data are not available. Because of the vast amount of effort which has been devoted to the problem of controls, this paper can illustrate only a few highlights in this respect. For more complete information, the reader is referred to the bibliography of reference 1 and references 2 to 51.

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[1]This paper, with some variations, was presented at the Fin-Stabilized Ammunition Symposium held on October 17, 1956, at Picatinny Arsenal, Dover, New Jersey.

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SYMBOLS

AR	aspect ratio, b^2/S_1
b	fin span, ft
C_{l_p}	roll damping-moment coefficient per radian of helix angle
C_{l_δ}	rolling-moment coefficient per degree of control deflection
c	fin chord in streamwise plane, ft
c_f	control chord in streamwise plane, ft
c_r	fin root chord at fuselage juncture, ft
d	body diameter, ft
h	projected height of spoiler above fin surface, ft
I	polar mass moment of inertia of round, slug-ft^2
k	exponential constant, sec^{-1}
L_c	rolling moment due to control, ft-lb
L_I	negative couple due to model inertia, ft-lb
L_p	negative rolling moment due to damping, ft-lb
M	Mach number
n	number of fin semispans
p	rolling velocity, radians/sec
$\dot{p}$	roll acceleration, $\frac{dp}{dt}$, radians/sec^2
pb/2V	fin-tip helix angle, radians
q	free-stream dynamic pressure, $\frac{1}{2}\rho V^2$, lb/sq ft
S	plan-form area of all fins to center line, sq ft

S_f total plan-form area of all control surfaces to center line, sq ft

S_1 plan-form area of two fins (one plane) to center line, sq ft

t fin thickness (unless otherwise noted), ft

V forward velocity, ft/sec

x longitudinal coordinate measured from fin leading edge, ft

δ control-surface deflection measured in streamwise plane, deg

ρ stream density, slugs/cu ft

ϕ flap trailing-edge angle measured between upper and lower flap surfaces in the streamwise plane, deg

DISCUSSION

Statement of the Problem

For reasons of simplicity, it is customary when dealing with pure roll of a finned projectile to express the rolling effectiveness of the control device in terms of the helix angle generated by the fin tips. From the helix angle it is then possible to determine the roll displacement per foot of range - a term often used by ammunition designers.

In order to gain a common understanding of the terms employed, reference is made to figure 1 which briefly outlines the derivation of the helix angle from the rolling moments of the system. The control in this case consists of canted fins all equally deflected to obtain pure roll. The resulting moments are given by the following equations:

$$L_c = C_{l_\delta}(\delta)qSb \tag{1}$$

$$-L_p = C_{l_p}(pb/2V)qSb \tag{2}$$

$$-L_I = I\dot{p} \tag{3}$$

A summation of these moments set equal to zero yields the usual solutions for both steady-state and transient roll conditions. In steady-state roll ($\dot{p} = 0$), the helix angle per degree of control deflection reduces to the simple expression:

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$$\frac{pb/2V}{\delta} = \frac{C_{l_\delta}}{-C_{l_p}} \tag{4}$$

from which the roll displacement per foot may be obtained by solving for p/V. Equation (4) shows the helix angle independent of fin scale, whereas the rolling velocity varies inversely with scale. The side effects of altitude or dynamic pressure on the helix angle are not apparent here until one considers the possible fin distortions caused by control or fin air loads. These so-called aeroelastic effects are frequently encountered with flap-type controls and will be examined further when this control is discussed.

Roll-response considerations.- The time lag for the round to reach some design level of roll rate is frequently of interest immediately after launching. In this connection the transient solution given by the following equation illustrates the factors which affect the response history:

$$\left(\frac{pb/2V}{\delta}\right)_{trans} = \frac{C_{l_\delta}}{-C_{l_p}}\left(1 - e^{-kt}\right) \tag{5}$$

where

$$k = -C_{l_p}\left(\frac{q}{V}\right)\left(\frac{Sb^2}{2I}\right)$$

and time t is given in seconds. For a given configuration the speed of response is related to both the magnitude of the control input $C_{l_\delta}(\delta)$ and to the terms in the exponential constant k. The time to reach some initial level of roll rate is largely a function of the control input since the input determines the initial roll acceleration. On the other hand, the time to reach the final steady-state condition is only a function of k which depends on flight conditions and the details of the basic configuration. The present paper will include some effects of changes in configuration on the steady-state time lag.

Control types and possible applications.- Of the conventional control types the deflected fin is still regarded as the simplest and most efficient aerodynamic device for producing roll. Other control arrangements are therefore justified only when necessary to satisfy certain design requirements for particular applications. If these requirements, for example, indicate a need for a fairly constant roll rate over the speed range or for a device which provides roll in but one direction even in reversed flow of propellant gases, then it appears that certain

flap, spoiler, or jet controls would be more suitable than deflected fins. These points will be covered in the following discussion of each control.

The experimental data on which the discussion is based were obtained primarily from NACA free-flight tests of fin-stabilized models incorporating these controls. The measurements were made near zero lift and under essentially steady-state roll conditions. The corresponding theoretical estimates of rolling effectiveness were calculated by means of equation (4) from ratios of the calculated coefficients C_{l_δ} and C_{l_p}. The deflection δ is measured in the streamwise plane, and the control rolling moments are assumed to increase linearly with deflection in accordance with linear theory.

Deflected Fin Controls

In discussing deflected fin controls, an attempt will be made to point out some effects of fin shape and aspect ratio on the steady-state and transient roll performance and to review the influence of fin-to-fin and fin-to-body interference.

Effects of plan-form shape.- The effect of deflected-fin shape is shown in figure 2 where the steady-state rolling effectiveness parameter $\frac{pb/2V}{\delta}$ is plotted against Mach number for several finned arrangements. The experimental results are shown by the solid and broken curves and slender cruciform wing-body theory (ref. 4), by the short dashed curve. It is noted that variations in fin shape for a given aspect ratio are not too significant insofar as the steady-state performance is concerned. Sweeping back the rectangular fin produced noticeable improvements by smoothing out the abrupt variations in rolling effectiveness with Mach number. These variations are attributed to the thick, sharp trailing-edge airfoil sections employed.

Effects of fin aspect ratio.- Figure 2 also indicates that the steady-state rolling effectiveness is not overly sensitive to differences in aspect ratio for a given type of plan form. This is in accord with theory which shows that while the average induced pressures over a deflected fin increase with aspect ratio, both the rolling and damping moments due to these pressures increase in about the same proportion so that their ratio (or steady-state helix angle) remains about the same. (See refs. 4, 5, 6, 20, 21, and 22.)

Probably of greater importance is the influence of aspect ratio on the transient response of the round. It will be recalled in connection with equation (5) that high damping-in-roll coefficients were significant

in reducing the time lag to achieve the steady-state roll condition. This is demonstrated more clearly in figure 3 which presents the calculated roll characteristics of a fin-stabilized projectile as rectangular fins of progressively greater span and aspect ratio are attached. The fin area and deflection remain constant, no interference effects are considered, and the mass of the projectile is assumed concentrated within the body of the round. All characteristics are in the form of ratios relative to the fin on the left. Increasing the aspect ratio from 2 to 10, or by a factor of 5, increased the rolling and damping moments by a factor of approximately 10. The steady-state helix angle remains essentially constant but the roll rate decreases as expected because of the increased span. The time lag to attain steady-state roll, meanwhile, was reduced by a factor of 10 because of increased damping coefficient and span. If it is desirable to recover the original roll rate with a larger control deflection, then this rate would be reached in one-tenth of the time by using the high-aspect-ratio rather than the low-aspect-ratio fins.

A precautionary comment might be added at this time regarding the method employed to obtain high aspect ratio. For example, in applications where a span increase is not feasible, some improvement in response may be obtained by increasing the fin chord, even though aspect ratio is reduced in the process. Figure 4 illustrates the result of this design maneuver for rectangular fins of constant span. Mach number 1.4 and the basic projectile are the same as assumed previously. By beginning with a small fin of high aspect ratio and gradually adding more chord (moving from right to left in fig. 4), note that the response time is improved somewhat. In the process, the reduction in damping coefficient caused by reducing the aspect ratio gradually offsets the benefit of added area until a point is reached where further increases in chord are not justified. Further calculations will show that this "optimum" chord increases with increased Mach number. Thus, the transient roll performance is significantly improved by employing higher fin aspect ratios if fin area is not sacrificed. On the other hand, increasing the fin area and chord may improve the response even though aspect ratio is reduced in the process. Probably a better alternative to increasing the chord, when span is limited, is to increase the area by adding more fins.

Effects of additional fins.- Some idea of the manner in which more fins affect the roll performance is provided by theory in figure 5. (See refs. 4 and 8.) The variations in moment coefficient and steady-state helix angle with Mach number are calculated for a delta-finned configuration. No body is considered and the fins are assumed to be of zero thickness. The number of fins are progressively increased from 2 to 4 and then to infinity to illustrate the limit case. The solid curves apply to 60° delta fins and the broken portions indicate the trend caused by a slight incremental increase in aspect ratio. Doubling the number of fins not quite doubles the moment coefficients, and therefore a

progressively smaller gain for each additional fin can be expected until the limit case is attained. In a practical case the limiting moments are probably less than indicated here and are, no doubt, obtained with fewer fins because of the viscous effects and physical limitations associated with fin thickness which theory does not consider. Momentwise and responsewise, more gain can be expected at higher Mach numbers by increasing the number of fins, particularly when fin aspect ratio is also increased. The helix angle is seen to diminish somewhat as more fins are added, and again in the limiting case the level actually obtained is probably lower than predicted for reasons mentioned earlier. Unfortunately the available experimental data which tend to bear out these predictions are limited to cases where only 2, 3, or 4 fins were tested. (See refs. 9, 24, and 26.)

Effect of body interference.- After examining the characteristics of isolated fins, it might be appropriate to determine the effect of body interference as the body diameter approaches the total fin span. In figure 6, the moment and steady-state helix-angle reduction factors are predicted for a cruciform configuration by slender wing-body theory. (See refs. 4, 23, 24, and 25.) These factors are plotted against the body diameter ratio and are expressed in terms of the fin-alone characteristics with no body. Notice that the presence of the body has little effect until it covers about a third of the fin span. Above this point the rolling and damping moments of the deflected fins fall off rapidly. The steady-state rolling velocity is least affected by body interference; however, an increase in response time can be expected. If more fins are added, another theory suggests that somewhat larger body diameters might be tolerated before the body effect becomes noticeable. (See ref. 8.) Whether this gain is significant in view of the increased fin-to-fin interference is questionable.

Deflected Flaps or Fin Segments

Figure 7 shows the experimental variation of rolling effectiveness with Mach number for a trailing-edge flap of a given area ratio on fins of different shape. The fin span, aspect ratio, airfoil section, and construction are all essentially constant, and under these conditions, the difference in shape is not too significant. Sweeping back the rectangular fin tends to reduce its effectiveness only at subsonic speeds. The tendency of the data to follow curves of constant roll rate suggests the use of flaps for obtaining a uniform rolling velocity at high speeds.

The primary fin variations which affect flap performance are thickness, section shape, aspect ratio, sweep, and flexibility. The flap variables naturally include span, chord, and deflection. Most of the discussion of fin variations will be centered around full-span flaps of a given size or area ratio and the data will correspond to an equivalent

rigid fin in order to divorce the aerodynamic effect of these variations from those caused by structural distortion due to flap loading. The effects of increasing the flap chord and fin flexibility will then be discussed. In all cases, the flap deflection will be defined as the angle in the streamwise plane between the flap mean line and the fin chord plane extended.

Effect of fin thickness and section shape.- At the top of figure 8 some rolling effectiveness curves are shown for a flap on rectangular fins of different thicknesses and thickness distributions. On the left the trend to be observed is the progressive loss in effectiveness accompanying the increase in airfoil thickness from 3 to 12 percent chord. On the right of the figure, when comparing fins of the same thickness, it can be seen that losses are also caused by variations in flap section shape. One method employed to account for both effects is to relate the flap effectiveness to the flap trailing-edge angle or that included angle between the upper and lower surfaces near the trailing edge. (See refs. 2 and 13.) The significance of this angle is demonstrated more clearly in the two cross plots at the bottom of the figure. In these plots, samples of data taken at two Mach numbers and obtained from tests of a variety of section shapes and thicknesses show the losses in effectiveness due to high trailing-edge angle. At supersonic speeds a good estimate of this loss is provided by modified linear theory of references 5 and 6. In fact an extension of this theory to deflected wedge-shaped fins or flaps accounts fairly well for the improved performance observed with simple wedge sections over more conventional shapes. (See refs. 3 and 15.)

Effects of fin aspect ratio and sweep.- For deflected-fin controls, it will be recalled that increasing the aspect ratio increased both the rolling and damping moments in about the same proportion. For flaps, however, theory shows that the rolling moments increase less rapidly with aspect ratio than do the damping moments. (See refs. 5 and 14.) Consequently, the helix angle or ratio of moments tends to decrease as aspect ratio increases. Theory further shows that as Mach number increases the observed flow becomes more two dimensional so that the effects of aspect ratio become less pronounced. Experimental results in figure 9 illustrate these trends for both the rectangular and triangular fin shapes. In either case it can be seen that increasing the fin aspect ratio reduces the rolling effectiveness but the differences become less prominent as the Mach number increases. For the rectangular fins, sweepback tends to reduce the effect of aspect ratio on flap effectiveness and to level off the variations in effectiveness with Mach number. (See ref. 2.)

Effect of increasing flap-chord ratio.- Now it is of interest to examine how flap effectiveness varies with flap size, particularly the manner in which its effectiveness approaches that of the completely

deflected fin. This is shown in figure 10 where the fraction of full-chord effectiveness is plotted against the flap chord ratio at two Mach numbers. The experimental points apply to flaps on fins of various shapes. (See refs. 2 and 15.) Two-dimensional or infinite-aspect-ratio theory is indicated by the broken curves while three-dimensional theory for rectangular or triangular fins of aspect ratio 4 is shown by the solid curve. At subsonic speeds, narrow flaps are quite effective, whereas, at supersonic speeds, effectiveness is roughly proportional to chord. The two theoretical curves at supersonic speeds are part of a trend which accounts for the relatively high effectiveness at low supersonic speeds of small flaps on very low-aspect-ratio fins. This trend becomes less pronounced as the Mach number increases.

Deflected-tip controls.- A control obtained by bending up the fin tip is illustrated in figure 11. (See ref. 14.) The theoretical characteristics of this device relative to the conventional deflected fin is indicated by the curve in all cases where the fin leading edges are supersonic. The experimental points for two test cases (see ref. 11) are shown by the symbols. The control deflections are again measured in the streamwise plane. Further information on tip controls may be found in references 2, 29, and 30.

Reversed-flow controls.- Two other controls of possible interest when reversed flows are encountered are canards and leading-edge flaps. At the top of figure 12 the canards, consisting of small canted surfaces located forward of the main fins, generate a downwash field of sufficient strength over the larger fins to cause negative roll. Since surfaces of this type perform in the regular manner in reversed flow as shown by the estimated curve (refs. 4 and 31), it is possible for them to produce roll in the same direction in either normal or reversed flow. The leading-edge flap in the lower plot also indicates promise over a limited Mach number range. (See ref. 28.)

Effects of fin flexibility.- In the preceding discussion we have reviewed the aerodynamic characteristics of flaps in connection with essentially rigid fins. It might be of interest, therefore, to have some idea of the losses in rolling effectiveness due to fin twist distortions which are caused by flap loads concentrated along the trailing edge. (See refs. 9, 16, 27, 32, 33, 34, and 35.) In this connection the calculated losses due to flexibility are presented in figure 13 for the case of a trailing-edge flap on unswept rectangular fins. The results are plotted against Mach number to show the effects of altitude, fin thickness, fin aspect ratio, and fin construction material. As might be expected, the losses at altitude are less due to a lower dynamic pressure q. In studying the other three plots, note that with steel fins at least 6 percent thick the losses at sea level over this Mach number range can be kept down to about 3 percent for the aspect-ratio-2 fins and to about 10 percent for the aspect-ratio-4 fins. If sweepback

is also incorporated, somewhat higher losses than shown here may be expected due to the additional fin-bending distortion (ref. 32).

Effects of body shape.- The last point to be discussed in connection with flaps is the possible effect of body shape on rolling effectiveness. (See fig. 14.) Since pinched-in afterbodies are not uncommon to ammunition design, it might be worth while to include the results of a test made at zero lift where the body shape was modified while flap size and body volume were maintained constant. (See ref. 15.) There was no significant change in the steady-state helix angle; however, again the steady-state helix angle is merely a ratio of moment coefficients and gives no indication on the actual effect of body shape on the magnitude of the moments involved. It might be added that substantial drag reductions were obtained by this modification.

Spoiler Controls

The top of figure 15 shows a sketch of a fin-spoiler arrangement which illustrates the approximate loading imposed on the fin by the spoiler and the resultant direction of positive roll.

Effect of chordwise location.- On the basis of this sketch, an improvement in effectiveness might be expected by locating the spoiler at the rear where less fin area is exposed to the negative pressures behind the spoiler. The data presented in the upper plot of figure 15 show some gain by this maneuver, particularly at transonic speeds. Probably more significant is to note that spoiler locations near midchord, for example, would produce roll in the same direction in reversed flow. This suggests their use in applications where such flows are encountered.

Effect of spoiler height.- One disadvantage of spoilers located forward of the trailing edge, is their ineffectiveness at low projections. (See refs. 36, 37, 38, and 42.) In some cases reversals in roll have been reported. An indication of this trend is shown by the bottom curve in the center plot (fig. 15) at subsonic speeds. This characteristic has been associated with a reattachment of the flow to the fin surface behind the spoiler which apparently occurs, particularly on thick fins, when the spoiler is lower than a critical height. (See ref. 37.) One investigation (ref. 37) has related this critical height to the angle between the fin surface and a line connecting the fin trailing edge with the top of the spoiler. Moving the spoiler to the rear or increasing its height generally improved the situation. (See refs. 15, 36, 37, and 42.)

Effect of fin thickness.- In the lower part of figure 15 the effect of fin thickness is shown to be not too significant for the zero lift

case considered. (See ref. 36.) There is some evidence to show that spoiler effectiveness is maintained to higher angles of attack on the thicker airfoil sections; this is particularly true at subsonic speeds.

Effect of fin flexibility.- In connection with thin wings which tend to be quite flexible, it has been found that the losses due to flexibility are less with spoilers than with trailing-edge flaps. This might be expected from the sketch at the top of figure 15 which shows a more favorable distribution of loads over the fin than is generally observed with flaps. As a result, the twisting moments and fin distortions are usually small for spoilers. (See ref. 43.)

Effect of spoiler shape.- Some comment on spoiler shapes which tends to reduce drag penalty might be in order if long-range projectiles are being considered. Figure 16 compares the relative effectiveness of the plain trailing-edge spoiler with that of a ramp having the same height but one-half the incremental drag. (See ref. 15.) The drag of the plain spoiler, incidentally, nearly doubled the drag of the basic cruciform wing-body combination. Locating the plain spoiler forward of the trailing edge caused negative roll, probably for reasons mentioned earlier. This should affect only the roll sense in reverse-flow applications.

Air-Jet Devices

The last control to be discussed is the jet device. A number of tests have shown that the total force obtained with jets in combination with fins may exceed the pure reaction force by a substantial margin. (See refs. 44, 45, and 51.)

Effects of chordwise location.- In most cases, the jet control has simply consisted of a number of closely spaced holes drilled in the fin surface and connected by a manifold or duct within the fin to inlets or some external source of air. The jet effectiveness has been found to be roughly proportional to flow rate, and trailing-edge locations seem to be the most satisfactory, although, more forward positions are also satisfactory for swept rectangular fins.

Effects of blowing direction.- Some idea of the potential of jets as a roll control is demonstrated in figure 17. By using air obtained from simple scoop inlets, test variations were made in the blowing direction which is either normal to the fin surface from a row of orifices, or in a spanwise direction from attached inlet stores. The normal blowing arrangement appears to be the most effective, although the store arrangement is probably the most practical for present ammunition designs. The jet controls tested were not too efficient compared to deflected fins, but some gains are possible by increasing the size of the inlet or using an auxiliary high-energy source of gas. In the test

case, the inlet and orifice areas were equal. The inlets occupied approximately 6 percent of the frontal area of the cruciform-fin model. The estimated thrust-force magnifications obtained with the jets blowing normal to the surface were of the order of 10 at subsonic speeds and 3 at supersonic speeds.

CONCLUDING REMARKS

The foregoing discussion has presented a rather brief summary of present information on the pure roll performance of several control devices. The selection of any one control over the others appears to be largely a matter of designer's choice with some exceptions depending on the roll requirements in a given situation.

Langley Aeronautical Laboratory,
National Advisory Committee for Aeronautics,
Langley Field, Va., December 12, 1956.

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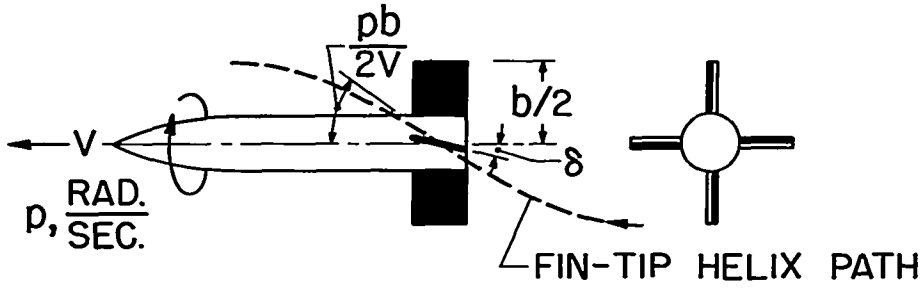

ROLLING MOMENTS ⊕:

DEFLECTED CONTROL: $L_c = C_{l_\delta}(\delta)qSb$ (1)

ROLL DAMPING: $-L_p = C_{l_p}(pb/2V)qSb$ (2)

INERTIAL COUPLE: $-L_I = I\dot{p}$ (3)

IN STEADY-STATE ROLL ($\dot{p} = 0$):

$$\frac{pb/2V}{\delta} = \frac{C_{l_\delta}}{-C_{l_p}} \tag{4}$$

IN TRANSITION FROM ZERO INITIAL ROLL:

$$\left(\frac{pb/2V}{\delta}\right)_{TRANS.} = \frac{C_{l_\delta}}{-C_{l_p}}\left[1-e^{-kt}\right] \tag{5}$$

WHERE $k = -C_{l_p}\left(\frac{q}{V}\right)\left(\frac{Sb^2}{2I}\right)$

Figure 1.- The finned projectile in pure roll.

[redacted]

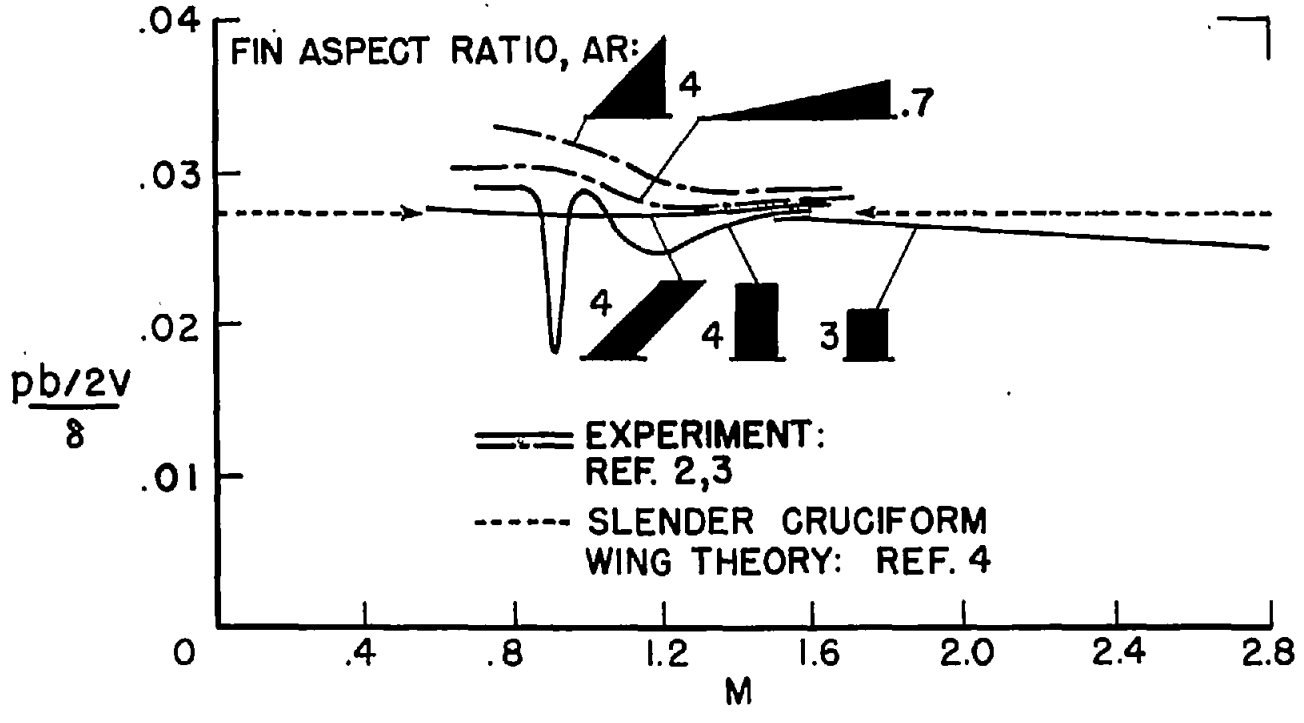

Figure 2.- Rolling effectiveness of deflected fins.

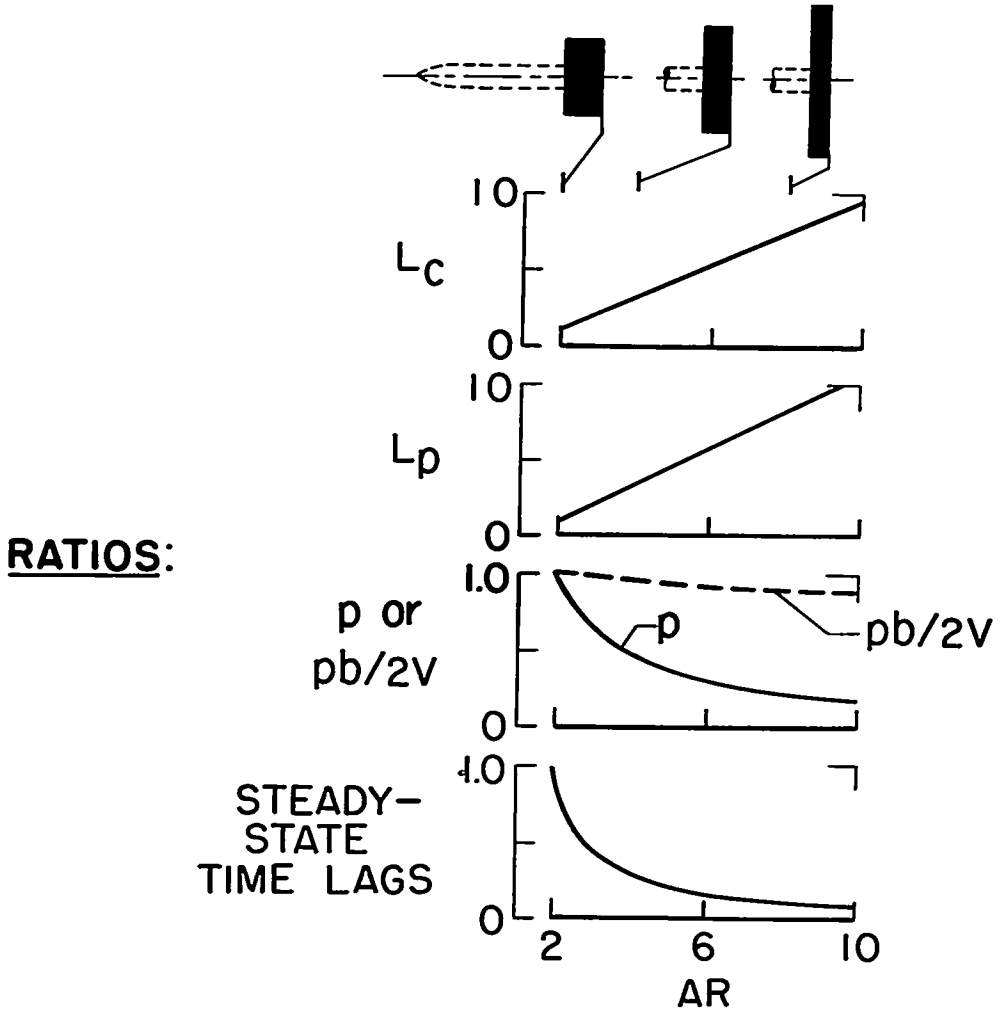

Figure 3.- Estimated effects of fin aspect ratio on the roll performance at sea level of a round with fins of constant area; 4 fins; S = 0.444 sq ft; I = 1/20 slug-ft^2; M = 1.4. Theory is from references 5 and 6.

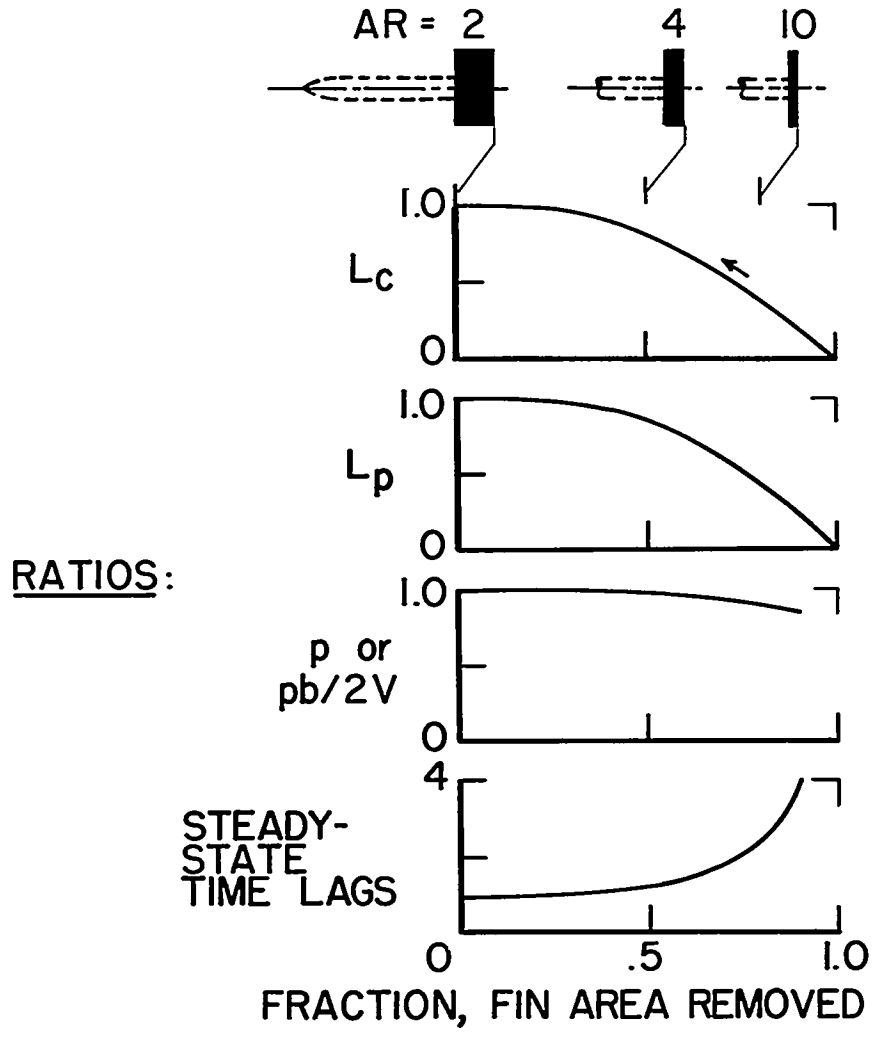

Figure 4.- Estimated effects of fin chord on the roll performance at sea level of a round with 4 fins of constant span; b = 2/3 ft; I = 1/20 slug-ft^2; M = 1.4. Theory is from references 5 and 6.

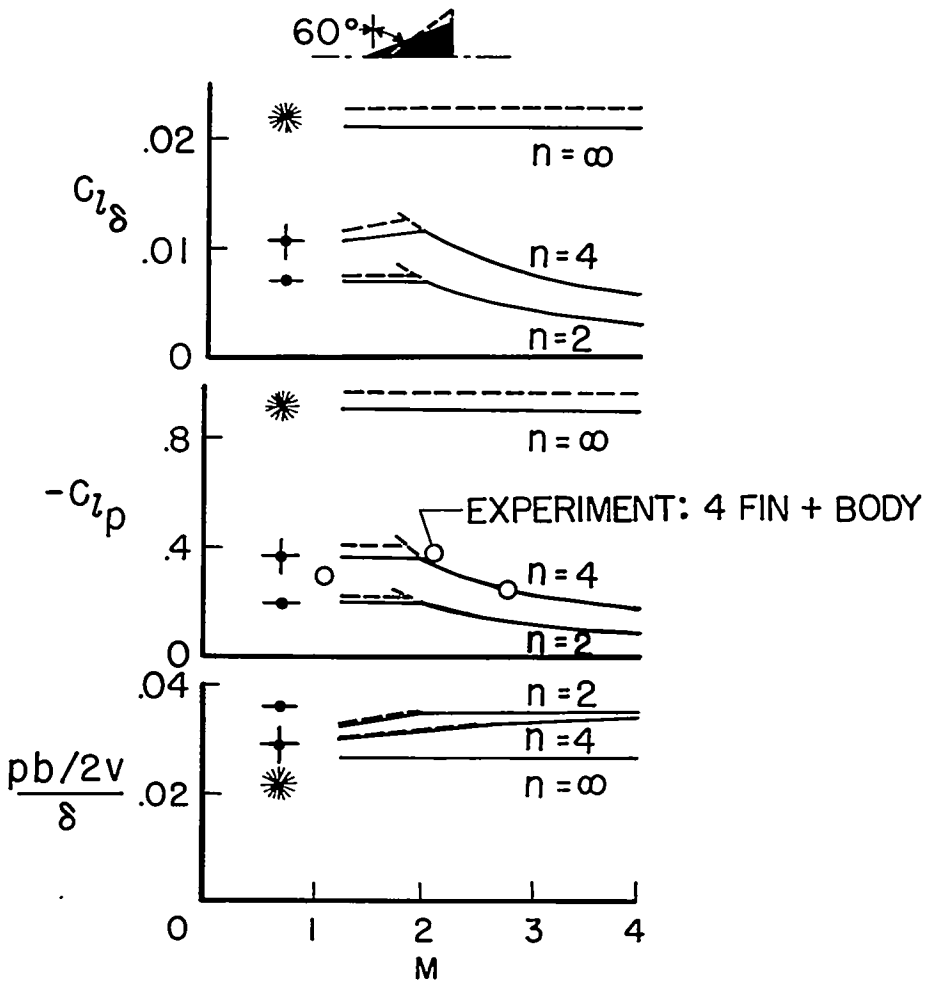

Figure 5.- Estimated effects of increasing number of fins on the rolling moments and effectiveness of deflected fins. No body considered coefficients are based on area of 2 fins. Theory is from Graham, reference 8, and data are from references 9 and 10.

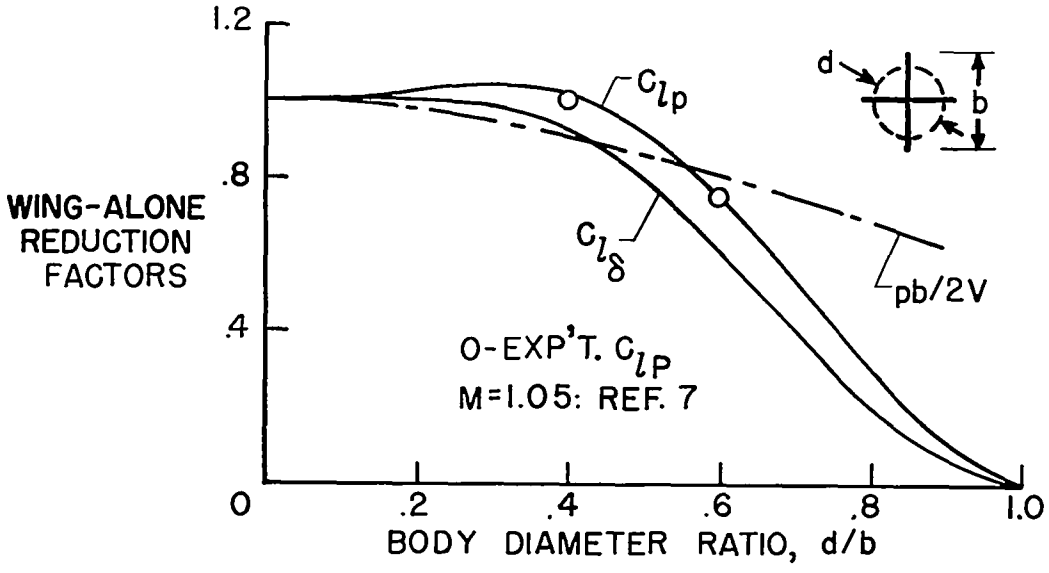

Figure 6.- Effect of body on deflected-fin rolling moments and effectiveness as predicted by slender wing-body theory, reference 4.

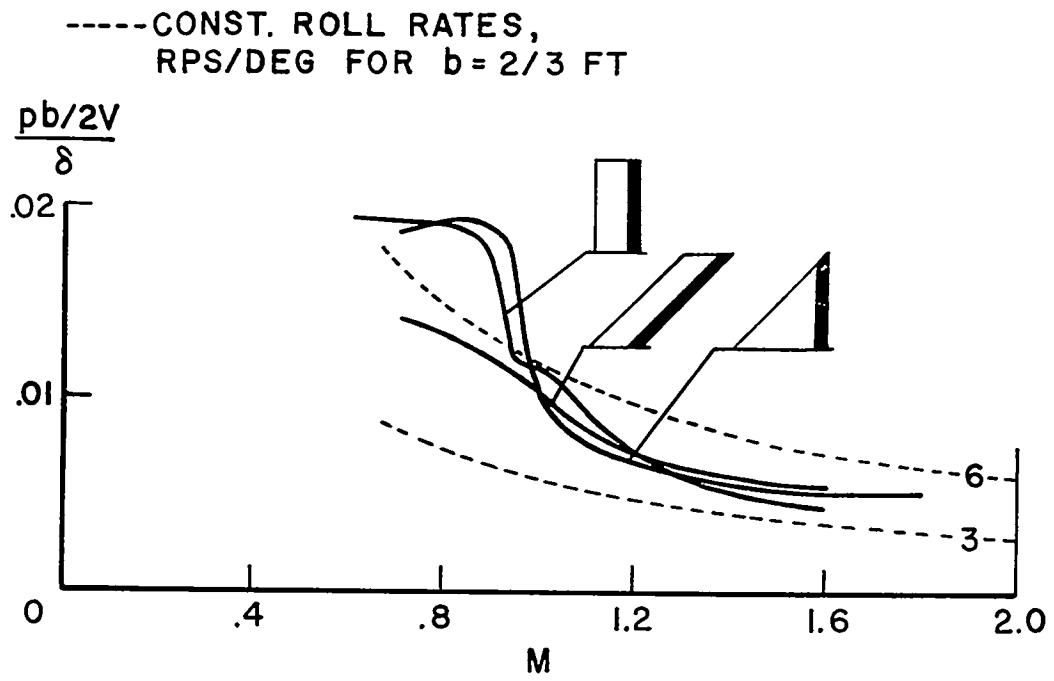

Figure 7.- Effects of fin shape and Mach number on flap rolling effectiveness; AR = 4; S_f/S = 0.2; aluminum fins. Data are from references 11 and 12.

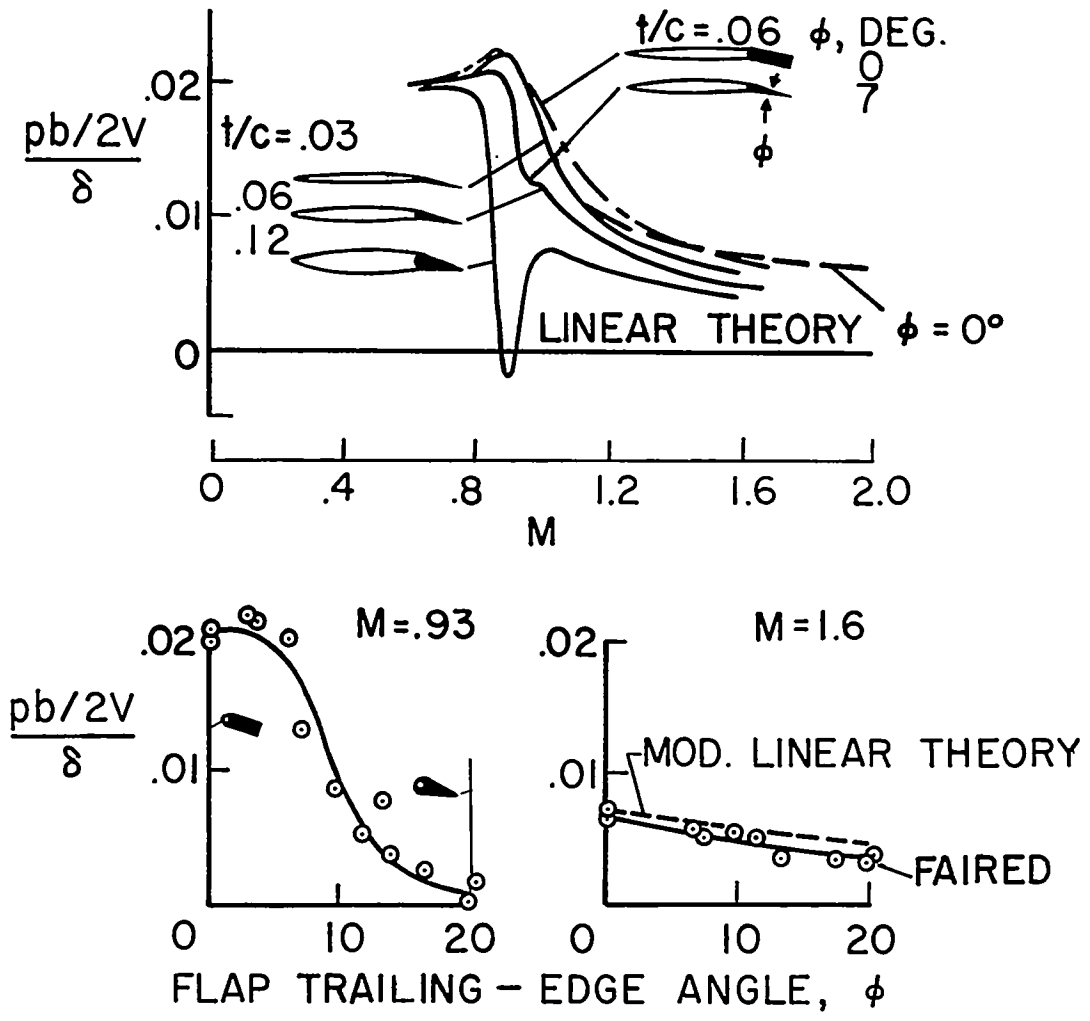

Figure 8.- Effects of fin section thickness and shape on the rolling effectiveness of 0.2 chord flaps on unswept rectangular fins; AR = 4; rigid fin. Theory is from references 5 and 6; data are from references 2 and 13.

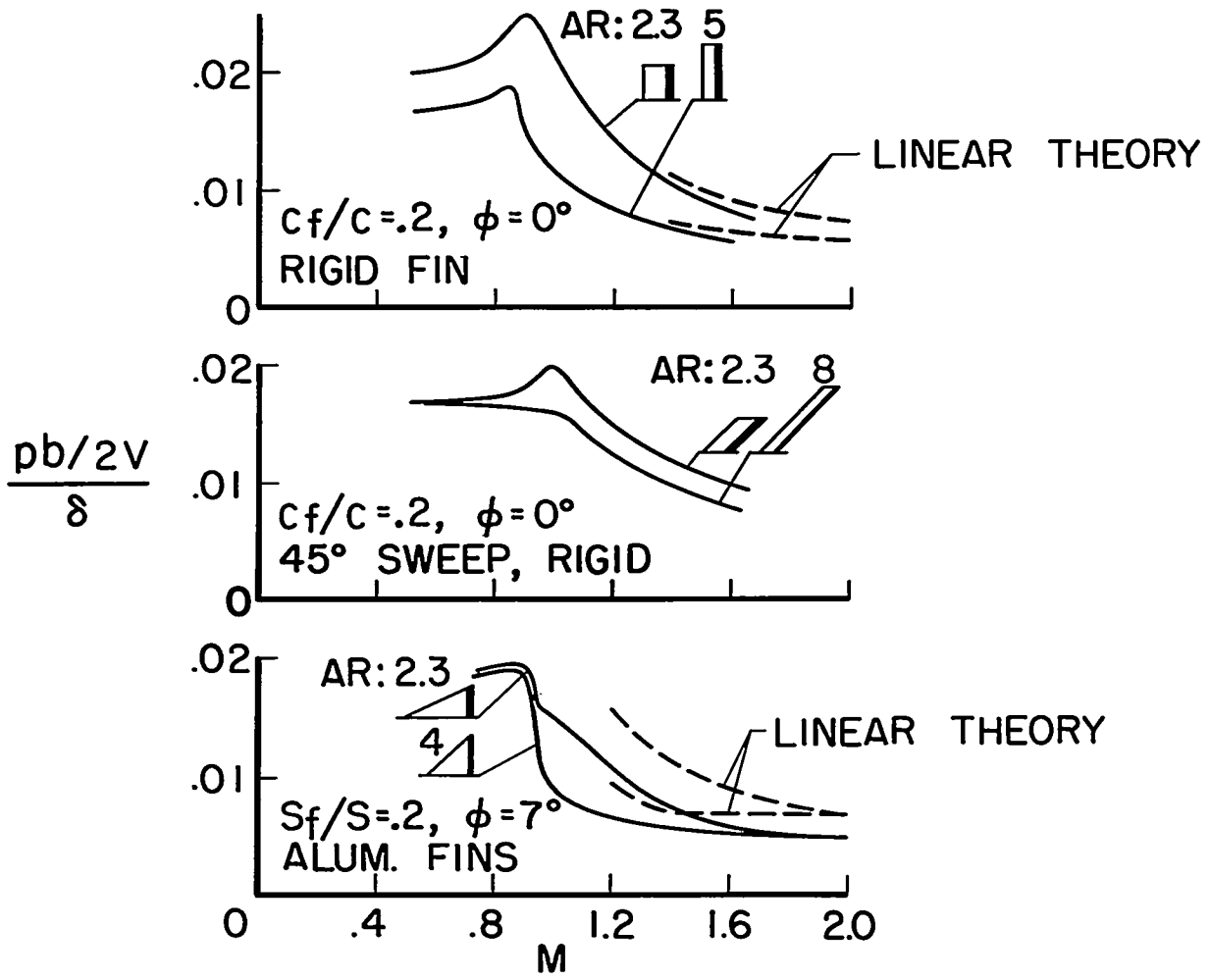

Figure 9.- Effects of aspect ratio on flap rolling effectiveness. Theory is from references 5, 6, and 14; data are from references 2 and 11.

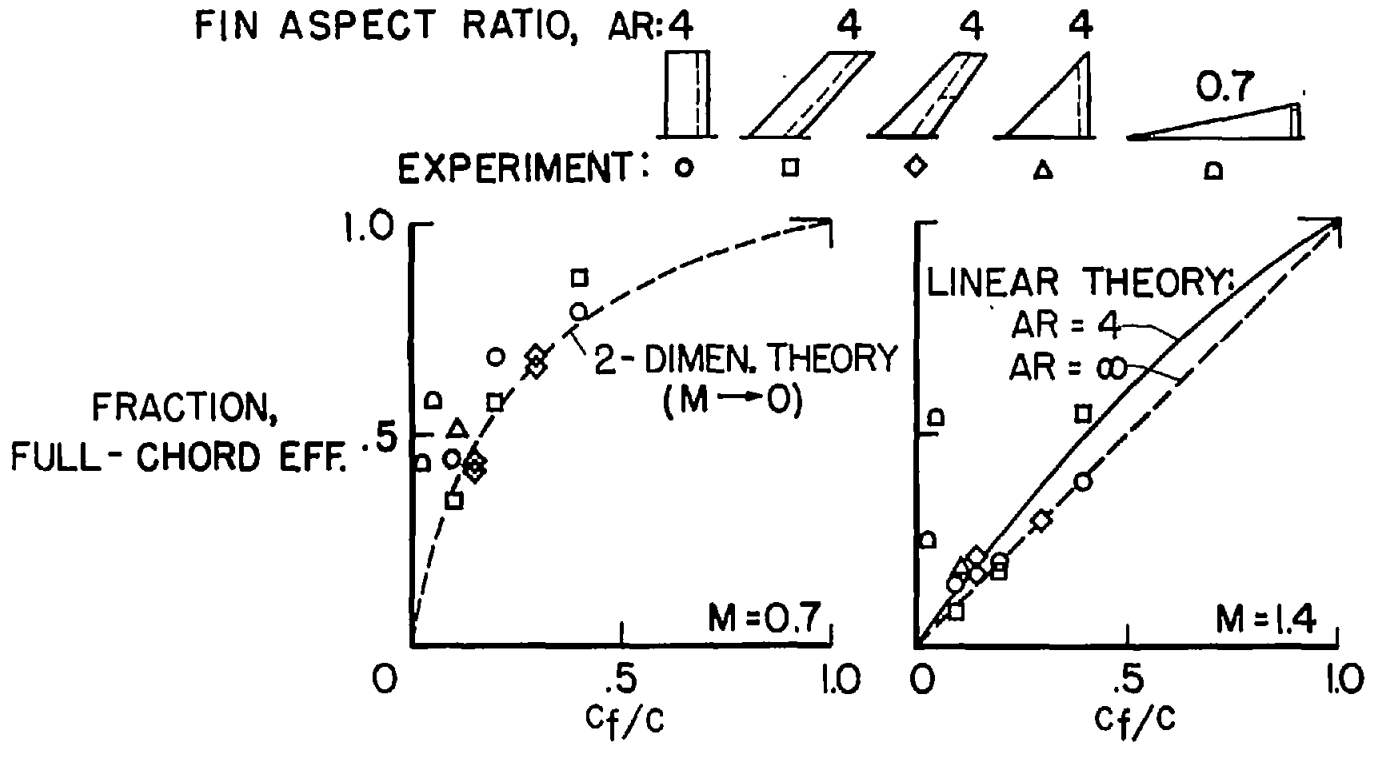

Figure 10.- Fraction of full-chord effectiveness obtained with flaps. Theory is from references 2, 5, 6, and 14; data are from references 2, 11, and 15.

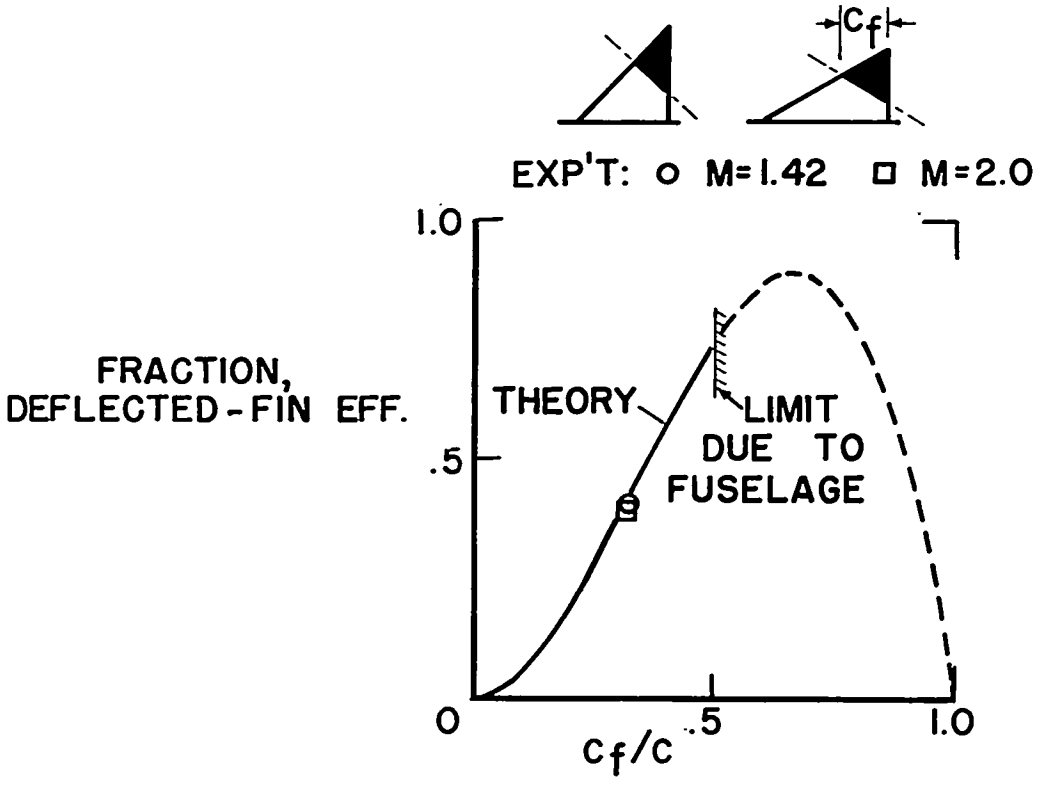

Figure 11.- Relative effectiveness of deflected-tip segments with supersonic leading edges. Theory is from references 6 and 14; data are from references 2 and 11.

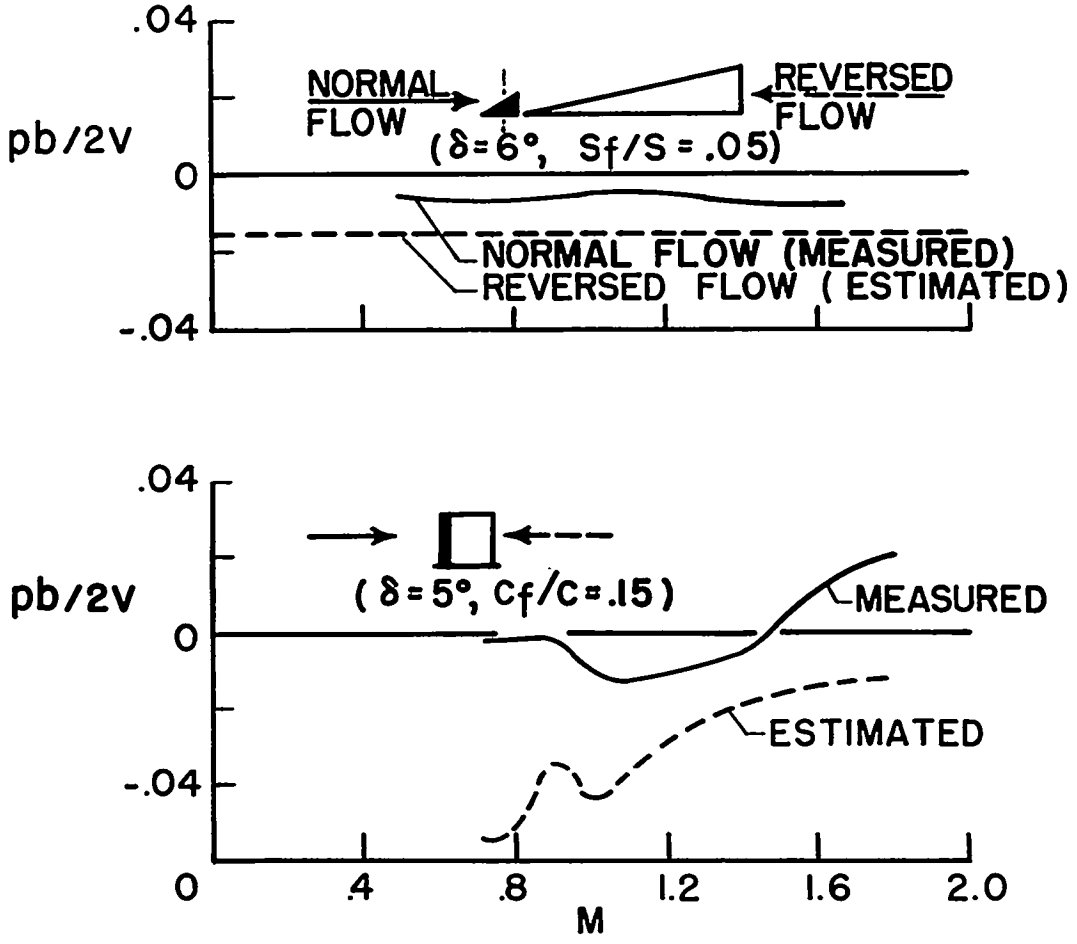

Figure 12.- Canards and leading-edge flaps as reversed-flow controls; references 4, 15, and 28.

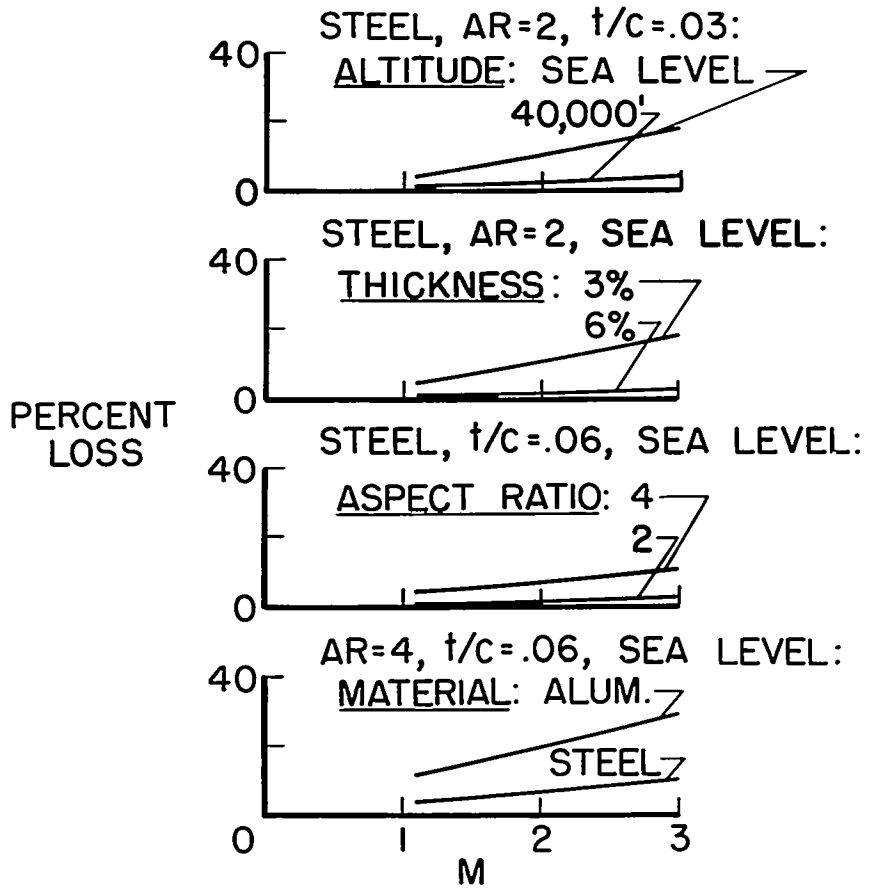

Figure 13.- Losses in rolling effectiveness due to fin flexibility for 0.2-chord, trailing-edge flaps on unswept rectangular fins, references 6 and 16.

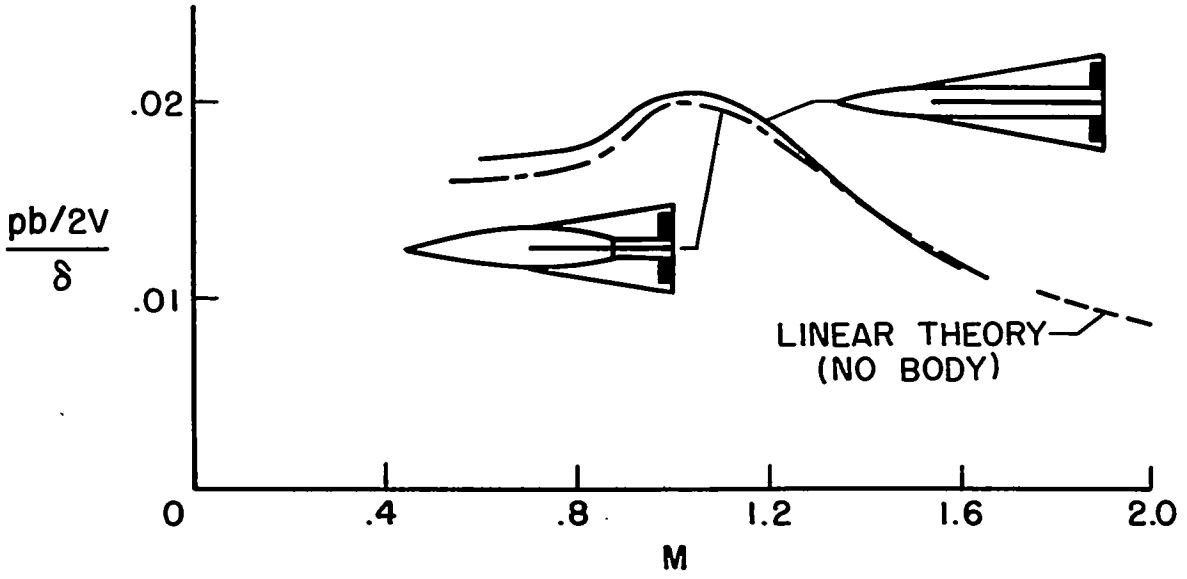

Figure 14.- Effect of a change in body shape on flap rolling effectiveness; 80° delta fins; $S_f/S \approx 0.10$. Data are from reference 15; theory is from references 6 and 14.

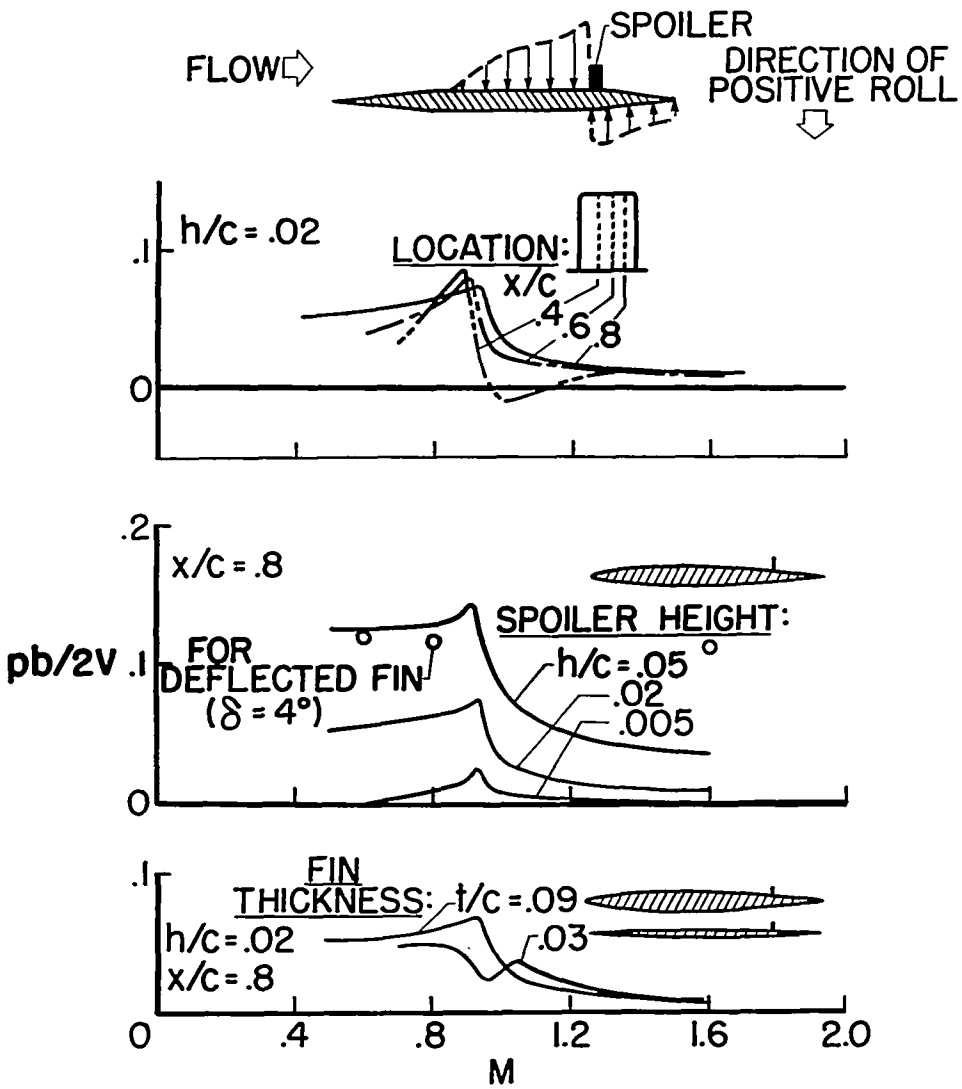

Figure 15.- Spoiler characteristics on unswept rectangular wings, references 17, 18, and 19.

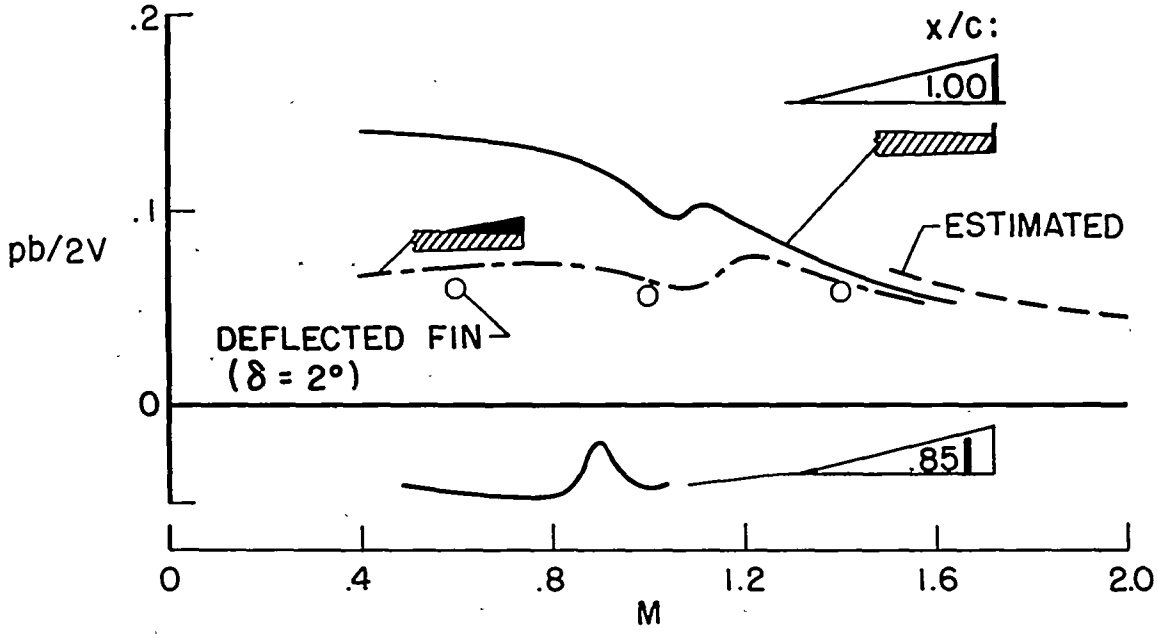

Figure 16.- Spoilers on 80° delta wings; $h/c_r = 0.008$. See reference 15.

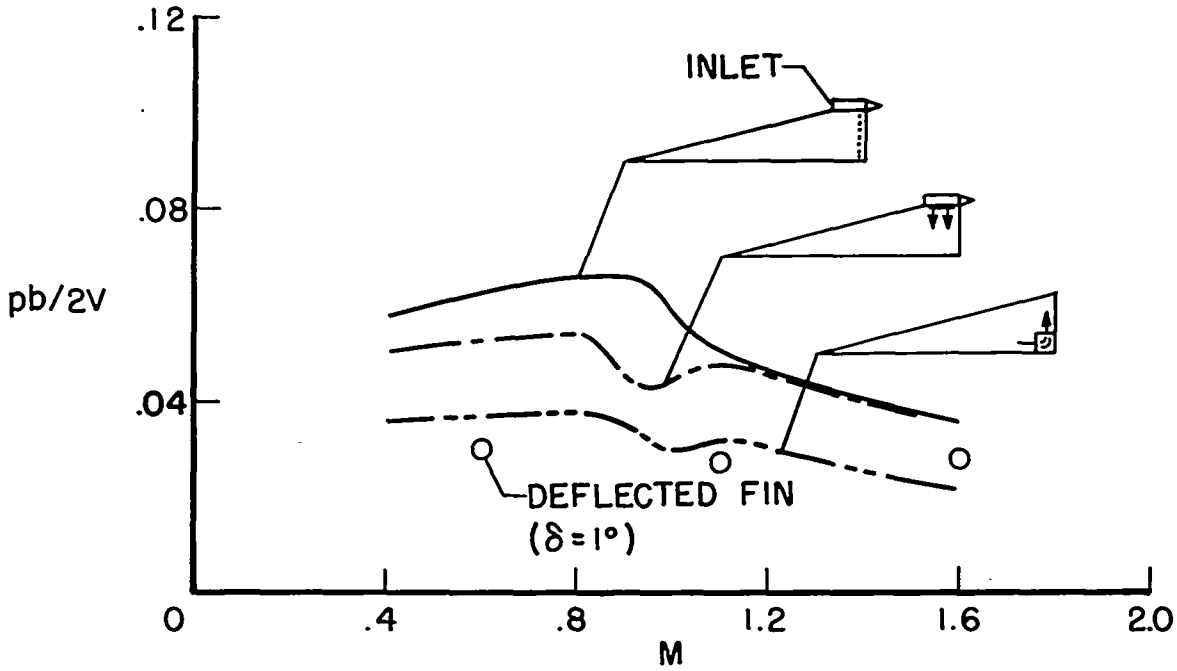

Figure 17.- Inlet-jet devices on 80° delta wings from reference 15.

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